

Scramble Round

Lexington High School

April 8, 2017

1. Compute

$$\frac{2+4+\cdots+2018}{1+3+\cdots+2017} + \frac{1+3+\cdots+2017}{2+4+\cdots+2018}.$$

2. Find the number of trailing zeros in

$$\prod_{i=1}^{2017} i!.$$

3. Compute the sum of the digits of 20^{17} .

4. Compute $1^2 + 2^2 + \cdots + 2017^2$.

5. Compute $\lfloor \sqrt{201700} \rfloor$.

6. Compute

$$\sum_{n=1}^{2017} \lfloor \sqrt{n} \rfloor.$$

7. Find the last three digits of $2017^{2016} - 2016^{2015} + 2015^{2014} - 2014^{2013}$.

8. Compute

$$\sum_{a,b \in \mathbb{Z}_{\geq 0}} \frac{1}{20^a \cdot 17^b}.$$

9. Compute 2017^2 .

10. Compute

$$\binom{20}{n=1} \binom{17}{n=1} = (1+2+3+\cdots+19+20)(1+2+3+\cdots+16+17).$$

11. Compute $1^2 - 2^2 + 3^2 - 4^2 + 5^2 \cdots + 2017^2$.

12. Compute the number of ordered pairs of nonnegative integers (m, n) which satisfy $20m + 17n \leq 340$.

13. Compute $20^4 - 17^4$.

14. Compute $\binom{20}{17}$.

15. For positive integers n , let $\sigma(n)$ denote the number of positive divisors of n . Find

$$\max_{1 \leq n \leq 2017} \sigma(n).$$

16. Compute the number of positive integers less than 2017 which are relatively prime to 2016.

17. Compute $\frac{1}{20} + \frac{1}{17} + \frac{1}{2017}$.

18. Find the number of primes between 1 and 217, inclusive.

19. Find the last three digits of 17^{2017} .

20. Compute $20 + 17$.

21. Compute $20^2 + 19^2 + 18^2 + 17^2$.

22. Compute the number of four-digit positive integers with the same digit sum as 2017.

23. Find the last three digits of $2017^{2017!} - 2017^{2017}$.

24. Compute

$$\sum_{n=1}^{2017} n = 1 + 2 + 3 + \cdots + 2016 + 2017.$$

25. Compute

$$\sum_{a, b \in \mathbb{Z}_{\geq 0}} \binom{20}{a} \binom{17}{b}.$$

26. Compute $20^2 - 17^2$.

27. Compute

$$\sum_{n=1}^{2017} n \cdot (-1)^n = -1 + 2 - 3 + 4 \cdots + 2016 - 2017.$$

28. When all of the numbers from 1 to 2017 are written out, how many times does the digit 1 appear?

29. Find the sum of all four-digit positive integers that share at least one common digit with 2017.

30. Compute the number of positive integers less than 2017 which are relatively prime to 2017.